- 1. D Limacon π/2
- A When you draw the point, it graphs in the second quadrant. By Pythagorean Theorem, I can find the radius to be 4. Using my special right triangles, I can see this is a 30-60-90 triangle, which makes the reference angle 60 degrees. From the polar axis, this angle is 120 degrees. (4, 120°)
- 3. B First we solve for how much of the circle is intercepted: $\frac{\pi/8 \, rad}{x \, degrees} = \frac{2\pi \, rad}{360 \, degrees}$; $x = 22.5 \, degrees \, or \frac{1}{16} \, of \, a \, circle$

Then we can multiple that length by 16 to find the full circumference. We are asked for diameter, so we must divide by pi.

E Because the length of the petals are 4, that is the coefficient. Because there are 8 petals, that means we use 4θ.Because the petals are not on the polar axis, we use the sine function.

$$r = 4\sin(4\theta)$$

5. C The rectangular (a) and polar (b) equations for the graphs given:

$$x^2 + y^2 = 9$$
; $r = 3$





**Remember that in a rectangular equation, it is equal to the radius squared!

6. A $\sqrt{41 - 10\sqrt{2} + 10\sqrt{6}}$ To find the distance between the following polar points: $\left(-4, \frac{\pi}{3}\right)$ and $\left(5, \frac{3\pi}{4}\right)$ we must use the law of cosines. The sides of the triangle are the two radii and the distance between the points. $c^2 = 5^2 + 4^2 - (2)(5)(4)cos105^\circ$. To find the cosine of 105 degrees, we must use the sum formula: $cos(105) = cos(60 + 45) = cos60cos45 - sin45sin60 = \sqrt{2} - \sqrt{6}/4$. $c^2 = 41 - 10(\sqrt{2} - \sqrt{6})$

polar

- 7. A Hyperbola symmetric about x-axis
- 8. D The missing information for a polar graph:

9. $D\left(\frac{3}{4} - \sqrt{3}, \frac{3\sqrt{3}}{4} - 1\right)$ To find the midpoint between the two polar points in rectangular form, first we must find the points in rectangular form: $x = rcos\theta \ y = rsin\theta$ yields $\left(\frac{3}{2}, \frac{3\sqrt{3}}{2}\right) and \left(-2\sqrt{3}, -2\right)$. Then we use the midpoint formula by just averaging the x coordinates and then averaging the y coordinates.

- 10. A To simplify $[-4 + 4i]^4 = [4\sqrt{2}cis \frac{3\pi}{4}]^4 = [(4\sqrt{2})^4 cis \frac{(4)3\pi}{4}] = 1024[cos\pi + isin\pi]$ ***Note that 3pi and pi are on the same location on the unit circle.
- 11. C $(3 + 3i)(-2 2\sqrt{3}i) = 12\sqrt{2}[cos285^\circ + isin285^\circ]$ and leave in the trigonometric form of a complex number.
- 12. B To find the largest wheel's angular speed: $\frac{4mi}{hr} \cdot \frac{5280ft}{1mi} \cdot \frac{2\pi rad}{4\pi ft} \cdot \frac{1hr}{60min}$ 176 To find the smallest wheel's angular speed: $\frac{4mi}{hr} \cdot \frac{5280ft}{1mi} \cdot \frac{2\pi rad}{\frac{4}{3}\pi ft} \cdot \frac{1hr}{60min} = 528$ 528-176=352
- 13. B From $\theta = \frac{-\pi}{12} = -15^{\circ}$ to his terminal value of $\theta = \frac{2\pi}{9} = 40^{\circ}$ is a difference of 55 degrees. $\frac{55}{360} 2\pi (14) = \frac{77\pi}{18}$ is the portion of the circumference that he traveled on the circle.

14. B $-\cos\theta = 1 + \cos\theta$; $2\cos\theta = -1$; $\cos\theta = -\frac{1}{2}$ $\theta = \frac{2\pi}{3}, \frac{4\pi}{3} \left(\frac{1}{2}, \frac{2\pi}{3}\right), \left(\frac{1}{2}, \frac{4\pi}{3}\right)Sum = 2\pi + 1$



- 15. B To find the $\cos^2 \theta$ of the point of intersection (r, θ) not at the pole for the circles with diameters of length 3 and $\frac{7}{4}$, $3sin\theta = \frac{7}{4}cos\theta$; $sin\theta = \frac{7}{12}cos\theta$; $sin^2\theta + cos^2\theta = 1$; $cos^2\theta = \frac{144}{193}$
- 16. C To classify the polar conic section, you must solve for the eccentricity. The 3 in the equation must be a 1 to determine this, so we will divide everything by 3. That makes the coefficient of the sine function 2/3, which is the eccentricity. We have an ellipse! Then to find the polar coordinates of its vertex/vertices, we notice the graph will be on the y-axis because of the sine function. The unit circle values on the y-axis are 90 and 270 degrees. By substituting those values into the equation, we get the vertices: $Ellipse(24, \pi/2), (24/5, 3\pi/2)$
- 17. A The area enclosed by the following set of parametric equations can be found using the basic formula for a circle, $A = \pi r^2$. I can see this is a circle from the identity: $\sin^2 x + \cos^2 x = 1$; $\left(\frac{x}{6}\right)^2 + \left(\frac{y}{6}\right)^2 = 1$; $x^2 + y^2 = 36$
- 18. C You can tell which of the following polar coordinates would not the Quadrant shown by using the approximation for pi is 3.14. 5 radians is more than half way around the circle, so (4,5) is not in the second quadrant.



- 19. A Hyperbolic
- 20. C) Lemniscate of Bernoulli

- 21. A A clock has hands with endpoints at polar coordinates $(-5, -\pi/12) = (-5, -15^{\circ} \text{ and } (3, -\pi/8) = (3, -22.5^{\circ}).$ You can graph an approximation to see the time to the nearest 15 minutes is 3:45.
- 22. B d = rt 310 = $r\left(\frac{2}{3}hour\right)$ r = 465mph

** The angles were unnecessary information. The plane is traveling along the path, so it is just a distance problem. If the plane farthest away reaches the axis, the plane closest will as well.

- 23. C To find the equation of the directrix on the graph of the following polar conic: $r = \frac{8}{1-cos\theta}$ first we should notice this is a parabola with eccentricity of 1. The equation has a cosine function, so I know the directrix has an equation with an "x". The equation is negative, so the directrix will be as well. The numerator is equal to ek, if e = 1, then k = 8. So I know in rectangular the equation of the directrix is x = -8. In polar, that equation is) $r = -8sec\theta$.
- 24. B A submarine's sonar sweeps an angle of $2\pi/9$ searching for ships. If an enemy ship is on the sonar screen, the probability that it will be within the swept area is just 1/9 because the entire unit circle is 2pi radians.

25. D $r = \frac{3}{1-sin\theta}$ The given information from the graph: y = -3 tells me that k = 3, the sign of the equation is negative, and the trig function will be a sine function. Because it is a parabola, the eccentricity is automatically 1.









- 27. A To solve the polar equation for any zeroes of the graph: $0 = cos^3\theta cos\theta = cos\theta(cos^2\theta 1); cos\theta = 0, -1, 1$ $\theta = 0, \frac{\pi}{2}, \pi, \frac{3\pi}{2}$
- 28. C To find the point of intersection of the polar graphs in rectangular coordinates: $r = 4csc\theta : rsin\theta = 4 : y = 4$ $r = -2sec\theta : rcos\theta = -2 : x = -2$ (-2, 4)
- 29. B The complex number 2 2i is graphed on the Argand plane forming a 45-45-90 special right triangle in the fourth quadrant. That makes the radius 2rt(2) and the angle 45 degrees. $(2\sqrt{2}, -\pi/4)$

30. D The slope of the line with the polar equation: $\theta = -\frac{2018\pi}{6} = -\frac{336\frac{1}{3}\pi}{1} = -\frac{1}{3}\pi$; $\tan\left(-\frac{1}{3}\pi\right) = -\sqrt{3}$